

Problem Solving

A Bridge to
Common Core Practices

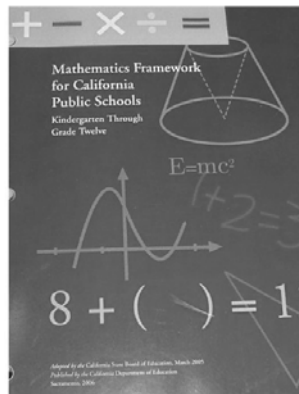
Phillippi/Wallis 2012

Welcome and Agenda

- ❖ Problem Solving and Math Reasoning
- ❖ Intro to Common Core Standards for Mathematical Practice
- ❖ Four-Step PS Process Defined
 - ❖ Understand, Plan, Solve, Check
- ❖ Problem Solving Models
- ❖ Applications
- ❖ Closure

Phillippi/Wallis 2012

Problem Solving and Mathematical Reasoning



Phillippi/Wallis 2012

Common Core Mathematical Practices

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

Phillippi/Wallis 2012

Similar but More Depth

- ❖ Comparison of MR Standards and Common Core Standards for Mathematical Practices
- ❖ Connections and Similarities
- ❖ Depth

Phillippi/Wallis 2012

Common Core Standards: Understanding the Mathematical *Practices* Standards

These Standards are not intended to be new names for old ways of doing business. They are a call to take the next step. It is time for states to work together to build on lessons learned from two decades of standards based reforms. It is time to recognize that standards are not just promises to our children, but promises we intend to keep.

— CCSS (2010, p.5)

Phillippi/Wallis 2012

Problem Solving

- ❖ Teaching students a **thinking process** for a problem the student does not know how to approach or solve.
 - ❖ Understand
 - ❖ Plan
 - ❖ Solve
 - ❖ Check
- ❖ The best way to improve problem solving skills is to **practice** problem solving with explicit instruction.
 - ❖ Verbal
 - ❖ Concrete
 - ❖ Pictorial
 - ❖ Symbolic

Phillippi/Wallis 2012

Understand

- ❖ Identify what is known by reading the problem carefully, sentence by sentence.
- ❖ Watch For the Operation
- ❖ Identify the question to answer or the task to perform.
 - ❖ What 7 coins make \$0.49?
 - ❖ List the seven coins that make \$0.49.

CC Math Practices

- ❖ Make sense of problems and persevere in solving them
- ❖ Look for and make use of structure
- ❖ Reason abstractly and quantitatively

Phillippi/Wallis 2012

Plan

- ❖ Identify the strategy to use that makes the most sense.
- ❖ Decide how the strategy will be used.
 - ❖ Visuals – What will you draw?
 - ❖ Act It Out – What materials will you use?
 - ❖ Make A Table – How will it be formatted?
 - ❖ And so on.....

CC Math Practices

- ❖ Make sense of problems
- ❖ Reason abstractly and quantitatively
- ❖ Use appropriate tools strategically
- ❖ Look for and make use of structure

Phillippi/Wallis 2012

Solve

- ❖ Show all your work (thinking) from the strategy.
- ❖ Constantly check your work against what is known
- ❖ Make sure the question is answered or the task is done.

CC Math Practices

- ❖ Use appropriate tools strategically
- ❖ Attend to precision
- ❖ Look for and express regularity in repeated reasoning

Phillippi/Wallis 2012

Check

- ❖ Compare the work to what is known.
- ❖ Make sure the question is answered or the task completed.
- ❖ Check that the answer makes sense.

CC Math Practices

- ❖ Construct viable arguments and critique the reasoning of others
- ❖ Model with mathematics

Phillippi/Wallis 2012

Primary PS Model

- ❖ Primary Problem:

I have 4 beads. I need 12 beads to make my bracelet.
How many more beads do I need?

- ❖ Understand
- ❖ Plan
- ❖ Solve
- ❖ Check

Phillippi/Wallis 2012

Upper Grade Model

- ❖ Davis has some marbles in his collection. His friend gave him 38 marbles. Davis now has 63 marbles altogether. What equation can be used to find the original amount of marbles m in Davis' collection?

- ❖ Understand
- ❖ Plan
- ❖ Solve
- ❖ Check

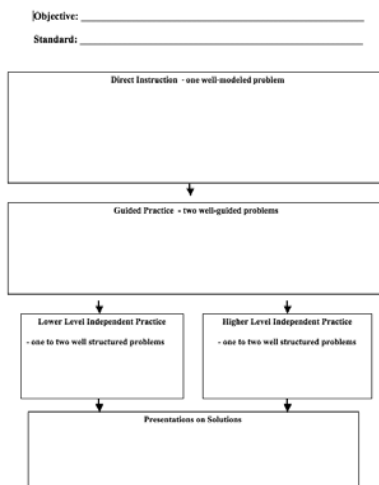
Phillippi/Wallis 2012

Practice the Process

Understand	Teacher Actions	Student Actions
<ul style="list-style-type: none"> Identify what is known by reading the problem carefully, sentence by sentence. Watch for the operation Identify the question to answer or the task to perform. 		
Plan <ul style="list-style-type: none"> Identify the strategy to use that makes the most sense. Decide how the strategy will be used. 		
Solve <ul style="list-style-type: none"> Show all your work from the strategy. Constantly check your work against what is known. Make sure the question is answered or the task is done. 		
Check <ul style="list-style-type: none"> Compare the work to what is known. Make sure the question is answered or the task completed. Check that the answer makes sense. 		

Phillippi/Wallis 2012

Putting All the Pieces Together



Phillippi/Wallis 2012

Closure



Phillippi/Wallis 2012